The Noether Theorems a century later

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Geometry, Dynamics and Mechanics online seminar

https://events.math.unipd.it/GDMSeminar/

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